

Question Number	Scheme	Marks
1.	<p>(a) Stratified</p> <p>(b) Label De-luxe rooms 1 – 20</p> <p>Using <i>random numbers</i> in range 1 – 20 select 2 rooms</p> <p>Repeat for Premier using 1 – 40 and select 4 rooms</p> <p>Repeat for Standard using 1 – 100 and select 10 rooms</p>	<p>B1 (1)</p> <p>B1</p> <p>B1 B1</p> <p>B1 (4)</p> <p>(5 marks)</p>
2.	<p>(a) <math>H_0: \mu_A = \mu_B</math>      <math>H_1: \mu_A \neq \mu_B</math></p> <p>standard error = <math>\sqrt{\frac{9.1^2}{100} + \frac{8.4^2}{120}} = 1.19</math> (awrt)</p> <p><math>\alpha = 0.01 \Rightarrow</math> CR: <math>z &lt; -2.5758</math> or <math>z &gt; 2.5758</math></p> <p><math>z = \frac{70.6 - 67.2}{1.19} = 2.86</math> (awrt)</p> <p>Since 2.86 is in the critical range, <math>H_0</math> is rejected. There is evidence of a difference in mean playing time.</p> <p>(b) Central Limit Theorem applies to enable normal distribution to be used.</p>	<p>B1 B1</p> <p>M1 A1</p> <p>B1 need both</p> <p>M1 A1</p> <p>A1ft (8)</p> <p>B1 (1)</p> <p>(9 marks)</p>
3.	<p>(a) <math>\bar{M} \sim N(80, \frac{2.6^2}{10})</math> or <math>N(80, 0.676)</math></p> <p>(b) <math>P(\bar{M} &lt; 78.5) = P(z &lt; \frac{78.5 - 80}{2.6/\sqrt{10}})</math></p> <p style="padding-left: 40px;"><math>= P(z &lt; -1.82)</math></p> <p style="padding-left: 40px;"><math>= 0.0344</math></p> <p>(c) Let <math>W =</math> weight of all 10 people</p> <p><math>W = M_1 + \dots + M_6 + F_1 + \dots + F_4</math></p> <p><math>E(W) = (6 \times 80) + (4 \times 59) = 716</math></p> <p><math>Var(W) = (6 \times 2.6^2) + (4 \times 1.9^2) = 55</math></p> <p><math>P(W &gt; 730) = P(z &gt; \frac{730 - 716}{\sqrt{55}})</math></p> <p style="padding-left: 40px;"><math>= P(z &gt; 1.89)</math></p> <p style="padding-left: 40px;"><math>= 0.0294</math></p>	<p>B1 B1 (2)</p> <p>M1</p> <p>A1</p> <p>A1 (3)</p> <p>B1</p> <p>B1</p> <p>M1 A1</p> <p>A1 (5)</p> <p>(10 marks)</p>

awrt = “anything which rounds to...”

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<p><b>4.</b> (a)</p>	<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 10%;"></th> <th style="width: 5%;">A</th> <th style="width: 5%;">B</th> <th style="width: 5%;">C</th> <th style="width: 5%;">D</th> <th style="width: 5%;">E</th> <th style="width: 5%;">F</th> <th style="width: 5%;">G</th> <th style="width: 5%;">H</th> <th style="width: 5%;">I</th> <th style="width: 5%;">J</th> </tr> </thead> <tbody> <tr> <td>Performance</td> <td>10</td> <td>5</td> <td>8</td> <td>3</td> <td>9</td> <td>6</td> <td>1</td> <td>4</td> <td>7</td> <td>2</td> </tr> <tr> <td>Dedication</td> <td>7</td> <td>6</td> <td>3</td> <td>5</td> <td>9</td> <td>10</td> <td>4</td> <td>2</td> <td>8</td> <td>1</td> </tr> </tbody> </table> <p><math>\Sigma d^2 = 70</math></p> $r_s = 1 - \frac{6 \times 70}{10 \times 99} = 0.576$		A	B	C	D	E	F	G	H	I	J	Performance	10	5	8	3	9	6	1	4	7	2	Dedication	7	6	3	5	9	10	4	2	8	1	<p>M1</p> <p>M1 A1</p> <p>M1 A1 (5)</p>
	A	B	C	D	E	F	G	H	I	J																									
Performance	10	5	8	3	9	6	1	4	7	2																									
Dedication	7	6	3	5	9	10	4	2	8	1																									
<p>(b)</p>	<p><math>H_0: \rho = 0; H_1: \rho \neq 0</math></p> <p><math>n = 10 \Rightarrow</math> critical value = 0.5636</p> <p>0.576 is in the critical region</p> <p>Evidence of correlation between performance and dedication.</p>	<p>B1 B1</p> <p>B1</p> <p>M1</p> <p>A1ft (5)</p>																																	
<p>(c)</p>	<p>Likely to be an element of judgement in grading.</p> <p>Dedication unlikely to be normally distributed.</p>	<p>B1 (1)</p> <p style="text-align: right;"><b>(11 marks)</b></p>																																	
<p><b>5.</b></p>	<table style="width: 100%; border-collapse: collapse;"> <tbody> <tr> <td style="width: 30%;">Expected Frequency</td> <td style="width: 15%;">Male:</td> <td style="width: 15%;">50.98</td> <td style="width: 15%;">27.85</td> <td style="width: 15%;">39.17</td> </tr> <tr> <td></td> <td>Female:</td> <td>57.02</td> <td>31.15</td> <td>48.83</td> </tr> </tbody> </table> <p><math>H_0</math>: no association between gender and facility</p> <p><math>H_1</math>: Association between gender and facility</p> $\sum \frac{(O - E)^2}{E} = \frac{(50.98 - 40)^2}{50.98} + \frac{(57.02 - 68)^2}{57.02} + \dots + \frac{(43.83 - 31)^2}{43.83}$ $= 12.7$ <p><math>\alpha = 0.05, \nu = 2 \Rightarrow</math> CR: <math>\chi^2 &gt; 5.991</math></p> <p>Evidence of association between gender and facility</p>	Expected Frequency	Male:	50.98	27.85	39.17		Female:	57.02	31.15	48.83	<p>M1 A1 A1</p> <p>B1</p> <p>B1</p> <p>M1 A1</p> <p>A1</p> <p>B1 B1</p> <p>A1ft (11)</p> <p style="text-align: right;"><b>(11 marks)</b></p>																							
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ft = follow through mark

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6.	<p>(a) <math>R = 43.76</math>; <math>S = 54.68</math>; <math>T = 43.76</math> using tables (OR <math>R = 43.75</math>; <math>S = 54.69</math>; <math>T = 43.75</math> using calculator)</p> <p>(b) <math>H_0</math>: Binomial model with <math>n = 8</math>, <math>p = 0.5</math> is suitable <math>H_1</math>: Binomial model with <math>n = 8</math>, <math>p = 0.5</math> is not suitable Amalgamation of data <math display="block">\sum \frac{(O - E)^2}{E} = 5.69 \text{ (awrt)}</math> <math>\alpha = 0.05</math>, <math>\nu = 6 \Rightarrow \text{CR: } \chi^2 &gt; \underline{12.592}</math> Since 5.69 is not in the critical region there is no evidence to reject <math>H_0</math>. The binomial model with <math>n = 8</math> and <math>p = 0.5</math> is a suitable model.</p> <p>(c) Apart from the expected values and <math>\sum \frac{(O - E)^2}{E}</math> being different, the degrees of freedom would have been reduced by 1 (<math>\nu = 5</math>).</p>	<p>M1 A1; B1 B1 (4)</p> <p>B1 (both) M1 M1 A1 <u>B1 B1</u> A1ft (7)</p> <p>B1 (1)</p> <p><b>(12 marks)</b></p>
7.	<p>(a) Cooling by subtracting 500 for each observation gives <math display="block">\text{Mean} = 500 + \frac{22}{10} = 502.2</math> <math display="block">\text{Variance} = \frac{1}{9} \left\{ 288 - \frac{22^2}{10} \right\} = 26.622</math></p> <p>(b) Limits are <math>502.2 \pm 1.6449 \times 5.0</math> (493.98, 510.42) [accept (494, 510)]</p> <p>(c) 95 % confidence limits are <math display="block">502.2 \pm 1.96 \times \frac{5.0}{\sqrt{10}}</math> (499, 505)</p> <p>(d) <math>H_0: \mu = 500</math> <math>H_1: \mu &gt; 500</math> <math>\alpha = 0.05 \Rightarrow \text{CR: } z &gt; 2.3263</math> <math display="block">z = \frac{503.9 - 500}{5.0 / \sqrt{15}} = 1.47</math> 1.47 is not in the critical region <math>\Rightarrow</math> no evidence to reject <math>H_0</math>; no evidence to suggest mean is greater than 500g</p>	<p>M1 A1 M1 A1 A1 (5)</p> <p>M1 A1 (2)</p> <p>M1 A1ft B1 (for 1.96) A1 A1 (5)</p> <p>B1 (both) B1 M1 A1 A1 ft (5)</p> <p><b>(17 marks)</b></p>