

Mark Scheme (Results) Summer 2010

GCE

GCE Statistics S3 (6691/01)

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.

Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information, please call our GCE line on 0844 576 0025, our GCSE team on 0844 576 0027, or visit our website at www.edexcel.com.

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our **Ask The Expert** email service helpful.

Ask The Expert can be accessed online at the following link:

<http://www.edexcel.com/Aboutus/contact-us/>

Summer 2010

Publications Code UA024774

All the material in this publication is copyright

© Edexcel Ltd 2010

Hypothesis Tests (Final M1A1)

For an incorrect comparison (e.g. probability with z value) even with a correct statement and/or comment award M0A0

For a correct or no comparison with more than one statement one of which is false
Award M0A0 (This is compatible with the principle above of contradictory statements being penalised)

Apply these rules to all questions

June 2010
 Statistics S3 6691
 Mark Scheme

Question Number	Scheme	Marks
Q1	<p>$H_0: \mu = 80, H_1: \mu > 80$</p> $z = \frac{83 - 80}{\frac{15}{\sqrt{100}}} = 2$ <p>$2 > 1.6449$ (accept 1.645 or better)</p> <p>Reject H_0 <u>or</u> significant result <u>or</u> in the critical region Managing director's claim is supported.</p>	<p>B1,B1</p> <p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p style="text-align: right;">7</p>
<p>2nd M1A1</p> <p>Critical Region</p>	<p>1st B1 for H_0. They must use μ not x, p, λ or \bar{x} etc</p> <p>2nd B1 for H_1 (must be > 80). Same rules about μ.</p> <p>1st M1 for attempt at standardising using 83, 80 and $\frac{15}{\sqrt{100}}$. Can accept \pm.</p> <p>May be implied by $z = \pm 2$</p> <p>1st A1 for + 2 only</p> <p>3rd B1 for ± 1.6449 seen (or probability of 0.0228 or better)</p> <p>2nd M1 for a correct statement about "significance" or rejecting H_0 (or H_1) based on their z value and their 1.6449 (provided it is a recognizable critical value from normal tables) <u>or</u> their probability (< 0.5) and significance level of 0.05. Condone their probability > 0.5 compared with 0.95 for the 2nd M1</p> <p>2nd A1 for a correct contextualised comment. Must mention "director" and "claim" <u>or</u> "time" and "use of Internet". No follow through.</p> <p>If no comparison or statement is made but a correct contextualised comment is given the M1 can be implied. If a comparison is made it must be <u>compatible</u> with statement otherwise M0 e.g. comparing 0.0228 with 1.6449 is M0 or comparing probability 0.9772 with 0.05 is M0 comparing -2 with - 1.6449 is OK provided a correct statement accompanies it condone -2 $>$ -1.6449 provided their statement correctly rejects H_0.</p> <p>They may find a critical region for \bar{X}: $\bar{X} > 80 + \frac{15}{\sqrt{100}} \times 1.6449 = \text{awrt } 82.5$</p> <p>1st M1 for $80 + \frac{15}{\sqrt{100}} \times (z \text{ value})$</p> <p>3rd B1 for 1.645 or better</p> <p>1st A1 for awrt 82.5</p> <p>The rest of the marks are as per the scheme.</p>	

Question Number	Scheme	Marks
Q2	<p style="text-align: center;">[$P \sim N(90,9)$ and $J \sim N(91,12)$]</p> <p>(a) $(J - P) \sim N(1, 21)$ $P(J < P) = P(J - P < 0)$ $= P\left(Z < \frac{0-1}{\sqrt{21}}\right)$ $= P(Z < -0.2182\dots)$ $= 1 - 0.5871 = 0.4129$ calculator (0.4136....)</p> <p>(b) $X = (J_1 + J_2 + \dots + J_{60}) - (P_1 + P_2 + \dots + P_{60})$ $E(X) = 60 \times 91 - 60 \times 90 = 60$ [stated as $E(X) = 60$ or $X \sim N(60, \dots)$] $\text{Var}(X) = 60 \times 9 + 60 \times 12 = 1260$ $P(X > 120) = P\left(Z > \frac{120-60}{\sqrt{1260}}\right)$ $= P(Z > 1.69030\dots)$ $= 1 - 0.9545 = 0.0455$</p>	<p>M1, A1</p> <p>dM1</p> <p>A1 (4)</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>M1</p> <p>A1 (5)</p> <p style="text-align: right;">9</p>
Use of means	<p>(a) 1st M1 for attempting $J - P$ and $E(J - P)$ or $P - J$ and $E(P - J)$ 1st A1 for variance of 21 (Accept $9 + 12$). Ignore any slip in μ here. 2nd dM1 for attempting the correct probability and standardising with their mean and sd. This mark is dependent on previous M so if $J - P$ (or $P - J$) is not being used score M0 If their method is not crystal clear then they must be attempting $P(Z < -ve \text{ value})$ or $P(Z > +ve \text{ value})$ i.e. their probability <u>after</u> standardisation should lead to a prob. < 0.5 so e.g. $P(J - P < 0)$ leading to 0.5871 is M0A0 unless the M1 is clearly earned. 2nd A1 for awrt 0.413 or 0.414</p> <p style="text-align: center;">The first 3 marks may be implied by a correct answer</p> <p>(b) 1st M1 for a clear attempt to identify a correct form for X. This may be implied by correct variance of 1260 B1 for $E(X) = 60$. Can be awarded even if they are using $X = 60J - 60P$. Allow $P - J$ and -60 1st A1 for a correct variance. If 1260 is given the M1 is scored by implication. 2nd M1 for attempting a correct probability and standardising with 120 and their 60 and 1260 If the answer is incorrect a full <u>expression</u> must be seen following through their values for M1 e.g. $P\left(Z > \frac{120 - \text{their } 60}{\sqrt{\text{their variance}}}\right)$. If using -60, should get $P\left(Z < \frac{-120 - -60}{\sqrt{\text{their variance}}}\right)$</p> <p>Attempt to use $\bar{J} - \bar{P}$ for 1st M1, $E(\bar{J} - \bar{P}) = 1$ for B1 and $\text{Var}(\bar{J} - \bar{P}) = 0.35$ for A1 Then 2nd M1 for standardisation with 2, and their 1 and 0.35</p>	

Question Number	Scheme	Marks
Q3 (a)	$E \sim N(0, 0.5^2)$ or $X \sim N(w, 0.5^2)$ $P(E < 0.6) = P\left(Z < \frac{0.6}{0.5}\right)$ or $P(X - w < 0.6) = P\left(Z < \frac{0.6}{0.5}\right)$ $= P(Z < 1.2)$ $= 2 \times 0.8849 - 1 = 0.7698$ awrt 0.770	M1 A1 (2)
(b)	$\bar{E} \sim N\left(0, \frac{1}{64}\right)$ or $\bar{X} \sim N\left(w, \frac{0.5^2}{16}\right)$ $P(\bar{E} < 0.3) = P\left(Z < \frac{0.3}{\frac{1}{8}}\right)$ or $P(\bar{X} - w < 0.3) = P\left(Z < \frac{0.3}{\frac{1}{8}}\right)$ $= P(Z < 2.4)$ $= 2 \times 0.9918 - 1 = 0.9836$ awrt 0.984	M1 M1, A1 A1 (4)
(c)	$35.6 \pm 2.3263 \times \frac{1}{8}$ (35.3, 35.9)	M1 B1 A1, A1 (4) 10
(a)	1 st M1 for identifying a correct probability (they must have the 0.6) and attempting to standardise. Need . This mark can be given for 0.8849 - 0.1151 seen as final answer. 1 st A1 for awrt 0.770. NB an answer of 0.3849 or 0.8849 scores M0A0 (since it implies no) M1 may be implied by a correct answer	
(b)	1 st M1 for a correct attempt to define \bar{E} or \bar{X} but must attempt $\frac{\sigma^2}{n}$. Condone labelling as E or X This mark may be implied by standardisation in the next line. 2 nd M1 for identifying a correct probability statement using \bar{E} or \bar{X} . Must have 0.3 and 1 st A1 for correct standardisation as printed or better 2 nd A1 for awrt 0.984 The M marks may be implied by a correct answer.	
Sum of 16, not means	1 st M1 for correct attempt at suitable sum distribution with correct variance ($= 16 \times \frac{1}{4}$) 2 nd M1 for identifying a correct probability. Must have 4.8 and 1 st A1 for correct standardisation i.e. need to see $\frac{4.8}{\sqrt{4}}$ or better	
(c)	M1 for $35.6 \pm z \times \frac{0.5}{\sqrt{16}}$ B1 for 2.3263 or better. Use of 2.33 will lose this mark but can still score $\frac{3}{4}$ 1 st A1 for awrt 35.3 2 nd A1 for awrt 35.9	

Question Number	Scheme	Marks																																
Q4 (a)	<table border="1" data-bbox="309 304 1238 555"> <tr> <td>Distance rank</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>Depth rank</td> <td>1</td> <td>2</td> <td>4</td> <td>3</td> <td>6</td> <td>7</td> <td>5</td> </tr> <tr> <td>d</td> <td>0</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td>2</td> </tr> <tr> <td>d^2</td> <td>0</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td>4</td> </tr> </table> <p data-bbox="225 629 347 678">$\sum d^2 = 8$</p> <p data-bbox="225 689 467 763">$r_s = 1 - \frac{6 \times 8}{7 \times 48}$</p> <p data-bbox="320 786 528 860">$= \frac{6}{7} = 0.857142$</p> <p data-bbox="1145 801 1289 837">awrt 0.857</p>	Distance rank	1	2	3	4	5	6	7	Depth rank	1	2	4	3	6	7	5	$ d $	0	0	1	1	1	1	2	d^2	0	0	1	1	1	1	4	<p data-bbox="1353 421 1401 456">M1</p> <p data-bbox="1353 495 1401 530">M1</p> <p data-bbox="1353 629 1437 665">M1A1</p> <p data-bbox="1353 725 1401 761">M1</p> <p data-bbox="1353 822 1401 857">A1</p> <p data-bbox="1474 860 1513 896">(6)</p> <p data-bbox="156 898 491 934">(b) $H_0 : \rho = 0, H_1 : \rho > 0$</p> <p data-bbox="225 943 676 978">Critical value at 1% level is 0.8929</p> <p data-bbox="225 994 895 1030">$r_s < 0.8929$ so not significant evidence to reject H_0,</p> <p data-bbox="225 1039 879 1075">The researcher's claim is not correct (at 1% level).</p> <p data-bbox="225 1084 831 1120"><u>or</u> insufficient evidence for researcher's claim</p> <p data-bbox="225 1128 1251 1164"><u>or</u> there is insufficient evidence that water gets deeper further from inner bank.</p> <p data-bbox="225 1173 1278 1209"><u>or</u> no (positive) correlation between depth of water and distance from inner bank</p> <p data-bbox="1353 898 1401 934">B1</p> <p data-bbox="1353 943 1401 978">B1</p> <p data-bbox="1353 994 1401 1030">M1</p> <p data-bbox="1353 1039 1422 1075">A1ft</p> <p data-bbox="1474 1077 1513 1113">(4)</p> <p data-bbox="1474 1182 1513 1218">10</p>
Distance rank	1	2	3	4	5	6	7																											
Depth rank	1	2	4	3	6	7	5																											
$ d $	0	0	1	1	1	1	2																											
d^2	0	0	1	1	1	1	4																											
(a)	<p data-bbox="225 1240 1054 1276">1st M1 for an attempt to rank the depths against the distances</p> <p data-bbox="225 1285 1050 1321">2nd M1 for attempting d for their ranks. Must be using ranks.</p> <p data-bbox="225 1330 919 1366">3rd M1 for attempting $\sum d^2$ (must be using ranks)</p> <p data-bbox="225 1375 890 1411">1st A1 for sum of 8 (or 104 for reverse ranking)</p> <p data-bbox="225 1420 1501 1496">4th M1 for use of the correct formula with their $\sum d^2$. If answer is not correct an expression is required.</p> <p data-bbox="225 1505 1497 1541">2nd A1 for awrt (\pm) 0.857. Sign should correspond to ranking (so use of 104 should get -0.857)</p>																																	
(b)	<p data-bbox="225 1574 1501 1610">1st B1 for both hypotheses in terms of ρ, H_1 must be one tail and compatible with their ranking</p> <p data-bbox="225 1619 715 1655">2nd B1 for cv of 0.8929 (accept \pm)</p> <p data-bbox="225 1664 1433 1700">M1 for a correct statement relating their r_s with their cv but cv must be such that $cv < 1$</p> <p data-bbox="225 1709 1437 1785">A1ft for a correct contextualised comment. Must mention "researcher" and "claim" <u>or</u> "distance (from bank)" and "depth (of water)"</p> <p data-bbox="363 1794 1123 1830">Follow through their r_s and their cv (provided it is $cv < 1$)</p> <p data-bbox="363 1839 719 1874">Use of "association" is A0</p>																																	

Question Number	Scheme					Marks																																																					
Q5	<table border="1" data-bbox="220 293 1214 465"> <thead> <tr> <th data-bbox="220 293 512 353">Finances</th> <th data-bbox="512 293 687 353">Worse</th> <th data-bbox="687 293 863 353">Same</th> <th data-bbox="863 293 1038 353">Better</th> <th data-bbox="1038 293 1214 353"></th> </tr> </thead> <tbody> <tr> <td data-bbox="220 353 512 394">Income</td> <td data-bbox="512 353 687 394"></td> <td data-bbox="687 353 863 394"></td> <td data-bbox="863 353 1038 394"></td> <td data-bbox="1038 353 1214 394"></td> </tr> <tr> <td data-bbox="220 394 512 434">Under £15 000</td> <td data-bbox="512 394 687 434">10.54</td> <td data-bbox="687 394 863 434">10.54</td> <td data-bbox="863 394 1038 434">12.92</td> <td data-bbox="1038 394 1214 434">34</td> </tr> <tr> <td data-bbox="220 434 512 474">£15 000 and above</td> <td data-bbox="512 434 687 474">20.46</td> <td data-bbox="687 434 863 474">20.46</td> <td data-bbox="863 434 1038 474">25.08</td> <td data-bbox="1038 434 1214 474">66</td> </tr> <tr> <td data-bbox="220 474 512 515"></td> <td data-bbox="512 474 687 515">31</td> <td data-bbox="687 474 863 515">31</td> <td data-bbox="863 474 1038 515">38</td> <td data-bbox="1038 474 1214 515">100</td> </tr> </tbody> </table> <p data-bbox="220 510 1086 551">H_0 : State of finances and income are independent (not associated)</p> <p data-bbox="220 555 1086 595">H_1 : State of finances and income are not independent (associated)</p> <table border="1" data-bbox="220 636 823 965"> <thead> <tr> <th data-bbox="220 636 339 734">O_i</th> <th data-bbox="339 636 488 734">E_i</th> <th data-bbox="488 636 679 734">$\frac{(O_i - E_i)^2}{E_i}$</th> <th data-bbox="679 636 823 734">$\frac{O_i^2}{E_i}$</th> </tr> </thead> <tbody> <tr> <td data-bbox="220 734 339 775">14</td> <td data-bbox="339 734 488 775">10.54</td> <td data-bbox="488 734 679 775">1.1358....</td> <td data-bbox="679 734 823 775">18.59..</td> </tr> <tr> <td data-bbox="220 775 339 815">11</td> <td data-bbox="339 775 488 815">10.54</td> <td data-bbox="488 775 679 815">0.0200....</td> <td data-bbox="679 775 823 815">11.48..</td> </tr> <tr> <td data-bbox="220 815 339 855">9</td> <td data-bbox="339 815 488 855">12.92</td> <td data-bbox="488 815 679 855">1.1893...</td> <td data-bbox="679 815 823 855">6.269..</td> </tr> <tr> <td data-bbox="220 855 339 896">17</td> <td data-bbox="339 855 488 896">20.46</td> <td data-bbox="488 855 679 896">0.5851...</td> <td data-bbox="679 855 823 896">14.12..</td> </tr> <tr> <td data-bbox="220 896 339 936">20</td> <td data-bbox="339 896 488 936">20.46</td> <td data-bbox="488 896 679 936">0.0103...</td> <td data-bbox="679 896 823 936">19.55..</td> </tr> <tr> <td data-bbox="220 936 339 976">29</td> <td data-bbox="339 936 488 976">25.08</td> <td data-bbox="488 936 679 976">0.6126...</td> <td data-bbox="679 936 823 976">33.53..</td> </tr> </tbody> </table> <p data-bbox="220 987 1326 1070">$\sum \frac{(O_i - E_i)^2}{E_i} = 3.553... \quad \text{or} \quad \sum \frac{O_i^2}{E_i} - 100 = 103.553... - 100 = 3.553... \quad (\text{awrt } \mathbf{3.55})$</p> <p data-bbox="220 1077 488 1117">$\nu = (3 - 1)(2 - 1) = 2$</p> <p data-bbox="220 1124 363 1164">cv is 5.991</p> <p data-bbox="220 1171 1118 1211">3.553 < 5.991 so insufficient evidence to reject H_0 <u>or</u> not significant</p> <p data-bbox="220 1218 1174 1258">There is no evidence of association between state of finances and income.</p>					Finances	Worse	Same	Better		Income					Under £15 000	10.54	10.54	12.92	34	£15 000 and above	20.46	20.46	25.08	66		31	31	38	100	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	14	10.54	1.1358....	18.59..	11	10.54	0.0200....	11.48..	9	12.92	1.1893...	6.269..	17	20.46	0.5851...	14.12..	20	20.46	0.0103...	19.55..	29	25.08	0.6126...	33.53..	<p data-bbox="1345 383 1401 454">M1 A1</p> <p data-bbox="1345 544 1401 584">B1</p> <p data-bbox="1345 786 1401 826">M1</p> <p data-bbox="1345 857 1401 898">A1</p> <p data-bbox="1345 1014 1401 1055">A1</p> <p data-bbox="1345 1086 1401 1126">B1</p> <p data-bbox="1345 1133 1401 1173">B1</p> <p data-bbox="1345 1180 1401 1220">M1</p> <p data-bbox="1345 1227 1401 1267">A1</p> <p data-bbox="1481 1294 1527 1335">10</p>
Finances	Worse	Same	Better																																																								
Income																																																											
Under £15 000	10.54	10.54	12.92	34																																																							
£15 000 and above	20.46	20.46	25.08	66																																																							
	31	31	38	100																																																							
O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$																																																								
14	10.54	1.1358....	18.59..																																																								
11	10.54	0.0200....	11.48..																																																								
9	12.92	1.1893...	6.269..																																																								
17	20.46	0.5851...	14.12..																																																								
20	20.46	0.0103...	19.55..																																																								
29	25.08	0.6126...	33.53..																																																								
	<p data-bbox="220 1350 1257 1424">1st M1 for some use of $\frac{\text{Row Total} \times \text{Col.Total}}{\text{Grand Total}}$. May be implied by correct E_i</p> <p data-bbox="220 1431 807 1471">1st A1 for all expected frequencies correct</p> <p data-bbox="220 1476 1437 1541">B1 for both hypotheses. Must mention “state” or “finances” and “income” at least once Use of “relationship” or “correlation” or “connection” is B0</p> <p data-bbox="220 1547 1493 1588">2nd M1 for at least two correct terms (as in 3rd or 4th column) or correct expressions with their E_i</p> <p data-bbox="220 1594 1501 1635">2nd A1 for all correct terms. May be implied by a correct answer. (2 dp or better - allow eg 1.13...)</p> <p data-bbox="220 1641 1469 1682">3rd M1 for a correct statement linking their test statistic and their cv. Must be χ^2 not normal.</p> <p data-bbox="220 1688 1469 1783">4th A1 for a correct comment in context - must mention “state” or “finances” and “income” condone “relationship” or “connection” here but not “correlation”. No follow through. e.g. “There is no evidence of a relationship between finances and income”</p>																																																										

Question Number	Scheme	Marks																																			
Q6	<table border="1"> <thead> <tr> <th>Distance from centre of site (m)</th> <th>0-1</th> <th>1-2</th> <th>2-4</th> <th>4-6</th> <th>6-9</th> <th>9-12</th> </tr> </thead> <tbody> <tr> <td>$b-a$</td> <td>1</td> <td>1</td> <td>2</td> <td>2</td> <td>3</td> <td>3</td> </tr> <tr> <td>No of artefacts</td> <td>22</td> <td>15</td> <td>44</td> <td>37</td> <td>52</td> <td>58</td> </tr> <tr> <td>$P(a \leq X < b)$</td> <td>$\frac{1}{12}$</td> <td>$\frac{1}{12}$</td> <td>$\frac{1}{6}$</td> <td>$\frac{1}{6}$</td> <td>$\frac{1}{4}$</td> <td>$\frac{1}{4}$</td> </tr> <tr> <td>$228 \times P(a \leq X < b)$</td> <td>19</td> <td>19</td> <td>38</td> <td>38</td> <td>57</td> <td>57</td> </tr> </tbody> </table>	Distance from centre of site (m)	0-1	1-2	2-4	4-6	6-9	9-12	$b-a$	1	1	2	2	3	3	No of artefacts	22	15	44	37	52	58	$P(a \leq X < b)$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{4}$	$228 \times P(a \leq X < b)$	19	19	38	38	57	57	M1 A1 A1
	Distance from centre of site (m)	0-1	1-2	2-4	4-6	6-9	9-12																														
	$b-a$	1	1	2	2	3	3																														
	No of artefacts	22	15	44	37	52	58																														
	$P(a \leq X < b)$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{4}$																														
	$228 \times P(a \leq X < b)$	19	19	38	38	57	57																														
	<table border="1"> <thead> <tr> <th>Class</th> <th>O_i</th> <th>E_i</th> <th>$\frac{(O_i - E_i)^2}{E_i}$</th> <th>$\frac{O_i^2}{E_i}$</th> </tr> </thead> <tbody> <tr> <td>0-1</td> <td>22</td> <td>19</td> <td>$\frac{9}{19} = 0.4736\dots$</td> <td>25.57...</td> </tr> <tr> <td>1-2</td> <td>15</td> <td>19</td> <td>$\frac{16}{19} = 0.8421\dots$</td> <td>11.84...</td> </tr> <tr> <td>2-4</td> <td>44</td> <td>38</td> <td>$\frac{36}{38} = 0.9473\dots$</td> <td>50.94...</td> </tr> <tr> <td>4-6</td> <td>37</td> <td>38</td> <td>$\frac{1}{38} = 0.0263\dots$</td> <td>36.02...</td> </tr> <tr> <td>6-9</td> <td>52</td> <td>57</td> <td>$\frac{25}{57} = 0.4385\dots$</td> <td>47.43...</td> </tr> <tr> <td>9-12</td> <td>58</td> <td>57</td> <td>$\frac{1}{57} = 0.0175\dots$</td> <td>59.01...</td> </tr> </tbody> </table>	Class	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	0-1	22	19	$\frac{9}{19} = 0.4736\dots$	25.57...	1-2	15	19	$\frac{16}{19} = 0.8421\dots$	11.84...	2-4	44	38	$\frac{36}{38} = 0.9473\dots$	50.94...	4-6	37	38	$\frac{1}{38} = 0.0263\dots$	36.02...	6-9	52	57	$\frac{25}{57} = 0.4385\dots$	47.43...	9-12	58	57	$\frac{1}{57} = 0.0175\dots$	59.01...	M1 A1
	Class	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$																																
	0-1	22	19	$\frac{9}{19} = 0.4736\dots$	25.57...																																
	1-2	15	19	$\frac{16}{19} = 0.8421\dots$	11.84...																																
2-4	44	38	$\frac{36}{38} = 0.9473\dots$	50.94...																																	
4-6	37	38	$\frac{1}{38} = 0.0263\dots$	36.02...																																	
6-9	52	57	$\frac{25}{57} = 0.4385\dots$	47.43...																																	
9-12	58	57	$\frac{1}{57} = 0.0175\dots$	59.01...																																	
<p>H_0: <u>continuous uniform</u> distribution <u>is</u> a good fit</p> <p>H_1: <u>continuous uniform</u> distribution <u>is not</u> a good fit</p>	B1																																				
$\sum \frac{(O_i - E_i)^2}{E_i} = \frac{313}{114} = 2.75 \quad \text{or} \quad \sum \frac{O_i^2}{E_i} - 228 = 230.745\dots - 228 = \dots \quad (\text{awrt } \mathbf{2.75})$	dM1A1																																				
$\nu = 6 - 1 = 5$	B1																																				
$\chi^2_5(0.05) = 11.070$ (ft their ν i.e. $\chi^2_\nu(0.05)$)	B1ft																																				
<p>2.75 < 11.070, insufficient evidence to reject H_0</p> <p>Continuous uniform distribution is a suitable model</p>	M1 A1																																				
	12																																				
	<p>1st M1 for calculation of at least 3 widths and attempting proportions/probs. <u>or</u> for 1:2:3 ratio seen</p> <p>1st A1 for correct probabilities</p> <p>2nd A1 for all correct expected frequencies</p> <p>2nd M1 for attempting $\frac{(O - E)^2}{E}$ or $\frac{O^2}{E}$, at least 3 correct expressions or values.</p> <p>Follow through their E_i provided they are not all = 38</p> <p>3rd A1 for a correct set of calcs - 3rd or 4th column. (2 dp or better and allow e.g. 0.94...)</p> <p>3rd dM1 dependent on 2nd M1 for attempting a correct sum or calculation (must see at least 3 terms and +)</p> <p>The first three Ms and As can be implied by a test statistic of awrt 2.75</p> <p>4th M1 for a correct statement based on their test statistic (> 1) and their cv (> 3.8)</p> <p>Contradictory statements score M0 e.g. "significant" do not reject H_0.</p> <p>5th A1 for a correct comment suggesting that continuous uniform model is suitable. No ft</p>																																				

Question Number	Scheme	Marks
Q7	(a) Label full time staff 1-6000, part time staff 1-4000 Use random numbers to select Simple random sample of 120 full time staff and 80 part time staff	M1 M1 A1 (3)
	(b) Enables estimation of statistics / errors for each strata <u>or</u> “reduce variability” <u>or</u> “more representative” <u>or</u> “reflects population structure” NOT “more accurate”	B1 (1)
	(c) $H_0: \mu_f = \mu_p, \quad H_1: \mu_f \neq \mu_p$ (accept μ_1, μ_2) $\text{s.e.} = \sqrt{\frac{21}{80} + \frac{19}{80}}, \quad z = \frac{52 - 50}{\sqrt{\frac{21}{80} + \frac{19}{80}}} = (2\sqrt{2})$ $= 2.828\dots$ (awrt 2.83)	B1 M1,M1 A1
	Two tailed critical value $z = 2.5758$ (or prob of awrt 0.002 (<0.005) or 0.004 (<0.01)) [2.828 > 2.5758 so] significant evidence to reject H_0 There is evidence of a difference in policy awareness between full time and part time staff	B1 dM1 A1ft (7)
	(d) Can use mean full time and mean part time ~ Normal	B1 B1 (2)
	(e) Have assumed $s^2 = \sigma^2$ or variance of sample = variance of population	B1 (1)
	(f) $2.53 < 2.5758$, not significant <u>or</u> do not reject H_0 So there is insufficient evidence of a difference in mean awareness	M1 A1ft (2)
	(g) Training course has closed the gap between full time staff and part time staff’s mean awareness of company policy.	B1 (1)
		17
	(a) 1 st M1 for attempt at labelling full-time and part-time staff. One set of correct numbers. 2 nd M1 for mentioning use of random numbers 1 st A1 for s.r.s. of 120 full-time and 80 part-time	
	(c) 1 st M1 for attempt at s.e. - condone one number wrong . NB correct s.e. = $\sqrt{\frac{1}{2}}$ 2 nd M1 for using their s.e. in correct formula for test statistic. Must be $\frac{\pm(52 - 50)}{\sqrt{\frac{p}{q} + \frac{r}{s}}}$ 3 rd dM1 dep. on 2nd M1 for a correct statement based on their normal cv and their test statistic 2 nd A1 for correct comment in context. Must mention “scores” or “policy awareness” and types of “staff”. Award A0 for a one-tailed comment. Allow ft	
	(d) 1 st B1 for mention of mean(s) <u>or</u> use of \bar{X} , provided \bar{X} clearly refers to full-time or part-time 2 nd B1 for stating that distribution can be assumed normal e.g. “mean score of the test is normally distributed” gets B1B1	
	(f) M1 for correct statement (may be implied by correct contextualised comment) A1 for correct contextualised comment. Accept “no difference in mean scores”. Allow ft	
	(g) B1 for correct comment in context that implies training was effective. This must be supported by their (c) and (f). Condone one-tailed comment here.	

Further copies of this publication are available from
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467
Fax 01623 450481

Email publications@linneydirect.com

Order Code UA024774 Summer 2010

For more information on Edexcel qualifications, please visit www.edexcel.com/quals

Edexcel Limited. Registered in England and Wales no.4496750
Registered Office: One90 High Holborn, London, WC1V 7BH