

**MARK SCHEME for the May/June 2011 question paper
for the guidance of teachers**

9231 FURTHER MATHEMATICS

9231/12

Paper 1, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

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Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol \surd implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.
PA –1	This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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Qu No	Commentary	Solution	Marks	Part Mark	Total
1	Any method including cover-up rule. Expresses all terms as differences. Finds sum.	$\frac{1}{(2r+1)(2r+3)} = \frac{1}{2} \left(\frac{1}{2r+1} - \frac{1}{2r+3} \right)$ $S_n = \frac{1}{2} \left(\left(\frac{1}{3} - \frac{1}{5} \right) + \left(\frac{1}{5} - \frac{1}{7} \right) + \dots + \left(\frac{1}{2n+1} - \frac{1}{2n+3} \right) \right)$ $= \frac{1}{6} - \frac{1}{2(2n+3)} \quad (\text{acf})$ $S_\infty = \frac{1}{6} \quad (\text{B0M1A1} \checkmark \text{ A0A1} \checkmark \text{ if signs reversed.})$	B1 M1A1 A1 A1	 4 1	[5]
2	Sum of roots. Sum of products in pairs. Factorises. Product of roots.	$\frac{\beta + \beta k + \beta k^2}{k} = -p$ $\frac{\beta^2}{k} + k\beta^2 + \beta^2 = q$ $\Rightarrow \beta \left(\frac{k^2 + k + 1}{k} \right) = -p \quad \text{and} \quad \beta^2 \left(\frac{k^2 + k + 1}{k} \right) = q$ $\Rightarrow \beta = -\frac{q}{p} \quad (\text{AG})$ $\beta^3 = -r$ $\Rightarrow -\frac{q^3}{p^3} = -r \Rightarrow rp^3 = q^3 \quad (\text{AG})$	B1 B1 M1 A1 B1 B1	 4 2	[6]
3 (i)	Reduces matrix to echelon form.	$\begin{pmatrix} 1 & 3 & -2 & 4 \\ 5 & 15 & -9 & 19 \\ -2 & -6 & 3 & -7 \\ 3 & 9 & -5 & 11 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 3 & -2 & 4 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$	M1A1		
(ii)	Obtains a set of equations.	$r(\mathbf{A}) = 4 - 2 = 2$ $x + 3y - 2z + 4t = 0$ $z - t = 0$	A1 B1	3	
	Finds basis vectors.	$\text{Basis is } \left\{ \begin{pmatrix} -2 \\ 0 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} -3 \\ 1 \\ 0 \\ 0 \end{pmatrix} \right\} \quad (\text{OE})$	M1A1	3	[6]

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4 (i)	Establishes initial result.	$f(n) + f(n+1) = 3^{3n} + 6^{n-1} + 3^{3n+3} + 6^n$ $= 3^{3n}(1+27) + 6^{n-1}(1+6)$ $= 28(3^{3n}) + 7(6^{n-1}) \quad (\text{AG})$	M1 A1	2	[6]
(ii)	States inductive hypothesis. Proves base case. Shows $P_k \Rightarrow P_{k+1}$. States conclusion.	$H_k: f(k) = 7\lambda$ $3^3 + 6^0 = 28 = 4 \times 7 \Rightarrow H_1 \text{ is true}$ $f(k+1) + f(k) = f(k+1) + 7\lambda = 28(3^{3k}) + 7(6^{k-1})$ $= 7\mu$ $\Rightarrow f(k+1) = 7(\mu - \lambda) \therefore H_k \Rightarrow H_{k+1}$ <p>(Hence by the principle of mathematical induction H_n is) true for all positive integers n.</p>	B1 B1 M1 A1	4	
5	Right-hand loop Left-hand loop Deduct 1 mark for extra loops ($r < 0$). Uses $A = \frac{1}{2} \int r^2 d\theta$ Uses double angle formula. Integrates. Inserts <i>any appropriate</i> limits which legitimately give the result.	Position and through pole and $(2, 0)$. Position and through pole and $(2, \pi)$. $A = \frac{1}{2} \int 4\cos^2\theta d\theta d\theta$ $= \int (\cos 4\theta + 1) d\theta \quad (\text{LNR})$ $= [\sin 4\theta + \theta] \quad (\text{LNR})$ <p>e.g. $[\sin 4\theta + \theta]_{-\frac{\pi}{4}}^{\frac{\pi}{4}} = \frac{\pi}{2}$</p>	B1B1 B1B1 M1 M1 A1 A1	4	[8]

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Qu No	Commentary	Solution	Marks	Part Mark	Total
6 (i)	Uses vector product to find vector perpendicular to both lines. Finds BA and its scalar product with unit perpendicular vector.	$\mathbf{n} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 4 & 3 & 0 \\ 4 & 0 & -1 \end{vmatrix} = -3\mathbf{i} + 4\mathbf{j} - 12\mathbf{j}$ $BA = \mathbf{i} + 10\mathbf{j} - 11\mathbf{j}$ $\text{perp.dist.} = \frac{-3 \times 1 + 4 \times 10 + 12 \times 11}{\sqrt{3^2 + 4^2 + 12^2}} = \frac{169}{\sqrt{169}} = 13$ <p style="text-align: center;">= 13 (AG) (No penalty for sign errors made in \mathbf{n}, which lead to correct result.)</p>	M1A1 M1A1	4	
(ii)		$\mathbf{p} = \begin{pmatrix} 8 + 4\lambda \\ 8 + 3\lambda \\ -7 \end{pmatrix} \quad \mathbf{q} = \begin{pmatrix} 7 + 4\mu \\ -2 \\ 4 - \mu \end{pmatrix}$ $PQ = \begin{pmatrix} -1 - 4\lambda + 4\mu \\ -10 - 3\lambda \\ 11 - \mu \end{pmatrix} = t \begin{pmatrix} -3 \\ 4 \\ -12 \end{pmatrix}$ $\Rightarrow t = -1 \quad \lambda = -2 \quad \mu = -1$ $\mathbf{p} = 2\mathbf{j} - 7\mathbf{k} \quad \mathbf{q} = 3\mathbf{i} - 2\mathbf{j} + 5\mathbf{k}$ <p>(Award B1B1B1 if t assumed to be ± 1 i.e. 3/5)</p>	B1 M1A1 M1 A1	5	[9]
6(ii)	Alternative Solution: Finds two parameter representation for PQ Uses scalar product between PQ and direction vector of at least one line and equates to zero Solves simultaneously. Obtains position vectors for P and Q	$\mathbf{p} = \begin{pmatrix} 8 + 4\lambda \\ 8 + 3\lambda \\ -7 \end{pmatrix} \quad \mathbf{q} = \begin{pmatrix} 7 + 4\mu \\ -2 \\ 4 - \mu \end{pmatrix}$ $PQ = \begin{pmatrix} -1 - 4\lambda + 4\mu \\ -10 - 3\lambda \\ 11 - \mu \end{pmatrix}$ $16\mu - 25\lambda = 34$ $17\mu - 16\lambda = 15$ $\mu = -1 \quad \lambda = -2$ $\mathbf{p} = 2\mathbf{j} - 7\mathbf{k} \quad \mathbf{q} = 3\mathbf{i} - 2\mathbf{j} + 5\mathbf{k}$	B1 M1A1 A1 M1A1 A1	7	
(i)	Obtains length of PQ .	$\sqrt{3^2 + (-4)^2 + 12^2} = 13 \quad (\text{AG})$	M1A1	2	[9]

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7	<p>Differentiates twice.</p> <p>Substitutes.</p> <p>Obtains v-x equation.</p> <p>Solves AQE</p> <p>Finds CF.</p> <p>Differentiates form for PI.</p> <p>Substitutes.</p> <p>Obtains PI</p> <p>Obtains GS</p> <p>Obtains y in terms of x (from a complete, if incorrect, GS).</p>	$v = y^3 \Rightarrow v' = 3y^2 y' \Rightarrow v'' = 3y^2 y'' + 6y(y')^2$ $\frac{1}{3}v'' - 2y(y')^2 + 2y(y'')^2 + \frac{2}{3}v' - 5v = 8e^{-x}$ $\Rightarrow \frac{d^2v}{dx^2} + 2\frac{dv}{dx} - 15v = 24e^{-x} \quad (\text{AG})$ $m^2 + 2m - 15 = 0 \Rightarrow m = -5, 3$ <p>CF: $Ae^{-5x} + Be^{3x}$</p> <p>PI: $v = ke^{-x} \Rightarrow v' = -ke^{-x} \Rightarrow v'' = ke^{-x}$</p> $ke^{-x} - 2ke^{-x} - 15ke^{-x} = 24e^{-x}$ $\Rightarrow -16ke^{-x} = 24e^{-x} \Rightarrow k = -\frac{3}{2}$ <p>GS: $v = Ae^{-5x} + Be^{3x} - \frac{3}{2}e^{-x}$</p> $y = \left\{ Ae^{-5x} + Be^{3x} - \frac{3}{2}e^{-x} \right\}^{\frac{1}{3}}$	<p>B1B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1√</p>	<p>4</p> <p>7</p>	[11]
8	<p>Finds characteristic equation and solves.</p> <p>Uses vector product (or equations) to find corresponding eigenvectors.</p> <p>Forms \mathbf{P} from eigenvectors and \mathbf{D} with fifth powers of eigenvalues on leading diagonal. Note: Columns of \mathbf{P} and \mathbf{D} can be permuted, but must match.</p>	$\text{Det}(\mathbf{A} - \lambda\mathbf{I}) = 0 \Rightarrow \lambda^3 - 4\lambda^2 - 11\lambda + 30 = 0$ $\Rightarrow \lambda = -3, 2, 5 \quad (\text{Any one})$ <p>(All three)</p> $\lambda = -3 \quad \mathbf{e}_1 = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 7 & -1 & 1 \\ -1 & 3 & -3 \end{vmatrix} = \begin{pmatrix} 0 \\ 20 \\ 20 \end{pmatrix} = t \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$ $\lambda = 2 \quad \mathbf{e}_2 = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 2 & -1 & 1 \\ -1 & -2 & -3 \end{vmatrix} = \begin{pmatrix} 5 \\ 5 \\ -5 \end{pmatrix} = t \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$ $\lambda = 5 \quad \mathbf{e}_3 = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ -1 & -1 & 1 \\ -1 & -5 & -3 \end{vmatrix} = \begin{pmatrix} 8 \\ -4 \\ 4 \end{pmatrix} = t \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix}$ $\mathbf{P} = \begin{pmatrix} 0 & 1 & 2 \\ 1 & 1 & -1 \\ 1 & -1 & 1 \end{pmatrix} \quad \mathbf{D} = \begin{pmatrix} -243 & 0 & 0 \\ 0 & 32 & 0 \\ 0 & 0 & 3125 \end{pmatrix}$	<p>M1A1</p> <p>A1</p> <p>A1</p> <p>M1A1</p> <p>A1</p> <p>A1</p> <p>B1√</p> <p>M1</p> <p>A1√</p>	<p>8</p> <p>3</p>	[11]

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9	Uses formulae for coords of centroid.	$\bar{x} = \frac{\int_1^4 x^{\frac{5}{2}} dx}{\int_1^4 x^{\frac{3}{2}} dx} \quad \bar{y} = \frac{\frac{1}{2} \int_1^4 x^3 dx}{\int_1^4 x^{\frac{3}{2}} dx}$	M1M1		
	Numerators.	$\left[\frac{2}{7} x^{\frac{7}{2}} \right]_1^4 = \frac{254}{7} \quad \left[\frac{1}{8} x^4 \right]_1^4 = \frac{255}{8}$	A1A1		
	Denominator.	$\left[\frac{2}{5} x^{\frac{5}{2}} \right]_1^4 = \frac{62}{5}$	B1		
	Obtains values. (Accept rational values.)	$\bar{x} = \frac{635}{217} (= 2.93) \quad \bar{y} = \frac{1275}{496} (= 2.57)$	M1A1	7	
	Differentiates y wrt x and squares.	$y = x^2 \Rightarrow y' = 2x \Rightarrow (y')^2 = 4x^2$	B1		
	Subs in arc length formula (LR).	$s = \int_5^{28} \sqrt{1 + \frac{9x}{4}} dx$	B1		
	Integrates.	$= \left[\frac{8}{27} \left(1 + \frac{9x}{4} \right)^{\frac{3}{2}} \right]_5^{28} \quad \text{or} \quad \left[\frac{1}{27} (4 + 9x)^{\frac{3}{2}} \right]_5^{28}$	M1A1		
Obtains printed result.	$= \frac{8^4 - 7^3}{27} \quad \text{or} \quad \frac{16^3 - 7^3}{27} = 139 \quad (\text{AG})$	A1	5	[12]	

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10	Puts $\cos^n x = \cos^{n-1} x \cdot \cos x$ and integrates by parts.	$I_n = \left[\cos^{n-1} x \sin x \right]_0^{\frac{\pi}{2}} + (n-1) \int_0^{\frac{\pi}{2}} \cos^{n-2} x \sin^2 x \, dx$	M1A1		
	Uses $\cos^2 x = 1 - \sin^2 x$ and obtains reduction formula.	$I_n = (n-1) \int_0^{\frac{\pi}{2}} (\cos^{n-2} x - \cos^n x) \, dx$ $\Rightarrow I_n = \frac{n-1}{n} I_{n-2} \quad (n \geq 2) \text{ (AG)}$	M1 A1	4	
	Uses mean value formula.	Mean value = $\frac{\int_a^b y \, dx}{b-a}$	M1		
	Transforms variable to t .	$= \frac{\int_0^{\frac{\pi}{2}} a \cos^3 t \cdot 3a \sin^2 t \cos t \, dt}{a}$	M1A1		
	Uses $\sin^2 t = 1 - \cos^2 t$ to write in a form where reduction formula can be used.	$= 3a \int_0^{\frac{\pi}{2}} \cos^4 t \sin^2 t \, dt$ $= 3a \int_0^{\frac{\pi}{2}} (\cos^4 t - \cos^6 t) \, dt \text{ (AG)}$	A1	4	
	Finds I_0 . Uses reduction formula to find I_4 and I_6 .	$I_0 = \frac{\pi}{2}$ or $I_2 = \pi/4$.	B1		
	(Or equivalent.)	$I_4 = \frac{3}{4} \cdot \frac{1}{2} \cdot \frac{\pi}{2} = \frac{3}{16} \pi$, $I_6 = \frac{5}{6} \cdot \frac{3}{16} \cdot \pi = \frac{5}{32} \pi$ (e.g. $I_6 = \frac{5}{6} I_4 \Rightarrow (I_4 - I_6) = \frac{1}{6} I_4$)	M1A1		
Substitutes in integral to find mean value.	Mean value = $\frac{3a}{32} \pi$	A1	4		
					[12]

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11	<p>EITHER</p> <p>Uses de Moivre's theorem and binomial theorem.</p> <p>(If line 1 missing, or no reference made to $\cos 3\theta$ and $\sin 3\theta$ being real and imaginary parts.)</p> <p>Equates real and imaginary parts.</p> <p>Uses $\tan A = \frac{\sin A}{\cos A}$</p> <p>States roots of $\tan 3\theta = 1$ between 0 and π.</p> <p>Obtains cubic equation and solves.</p> <p>Evaluates each root.</p>	$(\cos \theta + i \sin \theta)^3 = \cos 3\theta + i \sin 3\theta$ and $\cos^3 \theta + 3i \cos^2 \theta \sin \theta - 3 \cos \theta \sin^2 \theta - i \sin^3 \theta$	B1		
		Award B0M1A1M1M1A0 i.e.4/6	M1A1		
		$\sin 3\theta = 3 \cos^2 \theta \sin \theta - \sin^3 \theta$ $\cos 3\theta = \cos^3 \theta - 3 \cos \theta \sin^2 \theta$	M1		
		$\tan 3\theta = \frac{3 \cos^2 \theta \sin \theta - \sin^3 \theta}{\cos^3 \theta - 3 \cos \theta \sin^2 \theta}$	M1		
		$\therefore \tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$ (*) (AG)	A1	6	
		$\frac{\pi}{12}, \frac{5\pi}{12}, \frac{9\pi}{12} = \frac{3\pi}{4}$	B1 (one) B1 (all)	2	
		Put $\tan 3\theta = 1$ in (*) $\Rightarrow t^3 - 3t^2 - 3t + 1 = 0$	M1		
		Roots are $\tan \frac{\pi}{12}, \tan \frac{5\pi}{12}, \tan \frac{3\pi}{4}$	A1 (one) A1 (all)	3	
		$(t+1)(t^2 - 4t + 1) = 0$ $\Rightarrow t = -1, 2 \pm \sqrt{3}$	M1		
		$\tan \frac{3\pi}{4} = -1$ $\tan \frac{\pi}{12} = 2 - \sqrt{3}$	A1 (one)		
		$\tan \frac{5\pi}{12} = 2 + \sqrt{3}$	A1 (all)	3	
				[14]	

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11	OR				
(i)	Differentiates y wrt x .	$\frac{dy}{dx} = \frac{(x+3)(2x+\lambda) - (x^2 + \lambda x - 6\lambda^2)}{(x+3)^2}$ $= \frac{x^2 + 6x + 3\lambda + 6\lambda^2}{(x+3)^2}$	M1 A1		
	Uses discriminant and factorises.	$\frac{dy}{dx} = 0 \text{ has distinct roots if}$ $36 - 12\lambda - 24\lambda^2 > 0 \Rightarrow 3 - \lambda - 2\lambda^2 > 0$ $(3 + 2\lambda)(1 - \lambda) > 0$	M1 A1		
	Obtains result. (No equality.)	$\Rightarrow -\frac{3}{2} < \lambda < 1 \quad (\text{AG})$	A1	5	
(ii)	Uses division to obtain the form for recognition of oblique asymptote.	$\frac{x^2 + \lambda x - 6\lambda^2}{x+3} \equiv x + \lambda - 3 + \frac{9 - 3\lambda - 6\lambda^2}{x+3}$ (Tolerate error on remainder term.) \Rightarrow asymptotes are: $x = -3$ and $y = x + \lambda - 3$.	M1 B1 A1	3	
(iii)	For $0 < \lambda < 1$	Axes and asymptotes. Upper branch with minimum below x -axis. Lower branch with maximum.	B1 B1 B1	3	
(iv)	For $\lambda > 3$	Axes and asymptotes. (n.b. oblique asymptote has positive y intercept.) Left-hand branch. Right-hand branch.	B1 B1 B1	3	
	Deduct 1 mark overall for wrong forms At infinity.				[14]