

2 The cubic equation $2x^3 - 4x^2 + 3 = 0$ has roots α, β, γ . Let $S_n = \alpha^n + \beta^n + \gamma^n$.

(a) State the value of S_1 and find the value of S_2 . [3]

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(b) (i) Express S_{n+3} in terms of S_{n+2} and S_n . [1]

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(ii) Hence, or otherwise, find the value of S_4 . [2]

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5 The curve C has polar equation $r = \frac{1}{\pi - \theta} - \frac{1}{\pi}$, where $0 \leq \theta \leq \frac{1}{2}\pi$.

(a) Sketch C .

[3]

(b) Show that the area of the region bounded by the half-line $\theta = \frac{1}{2}\pi$ and C is $\frac{3 - 4 \ln 2}{4\pi}$. [6]

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A series of horizontal dotted lines for writing.

(c) Sketch C , stating the coordinates of the intersections with the axes.

[3]

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(d) Sketch the curve with equation $y = \left| \frac{x^2 - x - 3}{1 + x - x^2} \right|$ and find in exact form the set of values of x for which $\left| \frac{x^2 - x - 3}{1 + x - x^2} \right| < 3$.

[6]

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