



Cambridge International AS & A Level

CANDIDATE
NAME

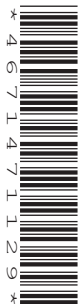
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CENTRE
NUMBER

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FURTHER MATHEMATICS

9231/21

Paper 2 Further Pure Mathematics 2

May/June 2021

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages.

1 (a) Given that a is an integer, show that the system of equations

$$ax + 3y + z = 14,$$

$$2x + y + 3z = 0,$$

$$-x + 2y - 5z = 17,$$

has a unique solution and interpret this situation geometrically.

[4]

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(b) Find the value of a for which $x = 1, y = 4, z = -2$ is the solution to the system of equations in part (a). [1]

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- (b) Use a similar method to find, in terms of n , a lower bound L_n for $\int_0^1 x^3 dx$. [4]

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- (c) Find the least value of n such that $U_n - L_n < 10^{-3}$. [2]

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