













A series of horizontal dotted lines for writing, spanning the width of the page.

5 Keira has two unbiased coins. She tosses both coins. The number of heads obtained by Keira is denoted by  $X$ .

(a) Find the probability generating function  $G_X(t)$  of  $X$ . [1]

.....  
.....  
.....  
.....  
.....  
.....  
.....

Hassan has three coins, two of which are biased so that the probability of obtaining a head when the coin is tossed is  $\frac{1}{3}$ . The corresponding probability for the third coin is  $\frac{1}{4}$ . The number of heads obtained by Hassan when he tosses these three coins is denoted by  $Y$ .

(b) Find the probability generating function  $G_Y(t)$  of  $Y$ . [3]

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....

The random variable  $Z$  is the total number of heads obtained by Keira and Hassan.

(c) Find the probability generating function of  $Z$ , expressing your answer as a polynomial. [3]

.....  
.....  
.....  
.....







