



## Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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CANDIDATE  
NUMBER

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**FURTHER MATHEMATICS**

**9231/12**

Paper 1 Further Pure Mathematics 1

**October/November 2021**

**2 hours**

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.

- 1 (a) Give full details of the geometrical transformation in the  $x$ - $y$  plane represented by the matrix  $\begin{pmatrix} 6 & 0 \\ 0 & 6 \end{pmatrix}$ . [1]

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 .....

Let  $\mathbf{A} = \begin{pmatrix} 3 & 4 \\ 2 & 2 \end{pmatrix}$ .

- (b) The triangle  $DEF$  in the  $x$ - $y$  plane is transformed by  $\mathbf{A}$  onto triangle  $PQR$ .

Given that the area of triangle  $DEF$  is  $13 \text{ cm}^2$ , find the area of triangle  $PQR$ . [2]

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 .....

- (c) Find the matrix  $\mathbf{B}$  such that  $\mathbf{AB} = \begin{pmatrix} 6 & 0 \\ 0 & 6 \end{pmatrix}$ . [2]

.....  
 .....

- (d) Show that the origin is the only invariant point of the transformation in the  $x$ - $y$  plane represented by  $\mathbf{A}$ . [4]

.....  
 .....

















(c) Sketch  $C$ .

[2]

(d) (i) Sketch the graphs of  $y = \left| \frac{x^2}{x-3} \right|$  and  $y = |x| - 3$  on a single diagram, stating the coordinates of the intersections with the axes. [4]

(ii) Use your sketch to find the set of values of  $c$  for which  $\left| \frac{x^2}{x-3} \right| \leq |x| + c$  has no solution. [1]

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